

# MATH 430 – Number Theory – SPRING 2010

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## Office Hours

Monday, Wednesday, Friday 11:00 to Noon  
And by appointment.

**Text** A Friendly Introduction to Number Theory 3<sup>rd</sup> edition by Joseph Silverman

**Syllabus** Chapters 1 to 19, 37, 39, 40. Also, there will be topics that are not in our textbook.

## Grading System

**Homework** 20%

Homework will be assigned and collected on a regular basis. Some problems will be for self or group study. Occasionally, I will assign problems that will be discussed the next class period. Extra credit is encouraged! See next page.

**Exams** 50%

There will be two in-class exams for your pleasure and enjoyment.  
Dates will be announced. ☺

**Final Exam** 30%

The Final Exam will be a take-home.  
Due: Tuesday, June 8 by 10:00 am.  
There is also a research paper option in lieu of the final exam. See next page.

## Grading Scale

A: 90%      B: 80%      C: 70%      D: 60%

Note: A minus grade is “-3%” and a plus grade is “+3%”.

E.g., 77% is a B- and 84% is a B+.

## Important Dates

Memorial Day Holiday      Monday, May 31

## Course Objectives

This course introduces students to selected topics in Number Theory that will reinforce the proof writing skills learned in MATH 260 (Logic & Sets). There is also a fair amount of computation involved that will reinforce the concepts and provide insight and intuition. Fundamentally, Number Theory is the study of divisibility, factorization and primes in the positive integers. This study will lead us to investigate all the integers (positive, negative & zero) and the rational numbers as well. Learner objectives, outcomes and skills include, but are not limited to:

- using the Euclidean Algorithm to find the gcd of a pair of positive integers and solve linear congruence equations
- understanding and using the Fundamental Theorem of Arithmetic to compute and solve a variety of problems
- applying the Chinese Remainder Theorem
- using Fermat's Little Theorem (FLT) and Euler's Generalization of FLT
- computing Pythagorean Triples and solving related problems
- solving linear congruence equations
- knowing some of the history, significance and role Fermat's Last Theorem has played in mathematics, especially, number theory.

## Comments

1. **Exams.** The exams I write for this course can be broken up into the following five components: (i) Definitions & Named Theorems (ii) Basic proofs

(iii) True – False (iv) Computations (v) Original proofs

(i) Logically equivalent statements for definitions and any theorem that has a name.

(ii) You should know any proof I give in class that is starred: **proof\***.

(iii) You know what true – false questions are like.

(iv) Routine computations similar to HW problems.

(v) Routine proofs similar to HW problems.

2. **Extra Credit.** Any challenging, at the very least non – trivial, problem from our text may serve as extra credit applied to the HW. These problems are not restricted to assigned chapters. Even better, if you have found your own pattern and you think you can prove it, submit it.

In general, consult with me on any problem you find interesting.

3. **Research Paper.** A research paper/project, minimum five pages and three works cited, can be submitted in lieu of the Final Exam. Deadline for topic approval is Friday, May 14. Team projects (two students) are welcome. Students must have a B or better to pursue this option. Details and paper/project suggestions will be given upon request.

4. **Homework Protocol** Ideally, homework should be done individually. However, your MATH 430 professor understands the value of collaborative work or receiving help from someone other than yours truly. All I ask of you is that you document those from whom you received assistance. In these cases please write at the beginning of your homework paper:

(i) “I received help (assistance, hints) on problem(s) \_\_\_\_\_ from \_\_\_\_\_.”

or

(ii) “ ‘Ethan’ and I worked together on problem(s) \_\_\_\_\_.”

If you receive help from a tutor (private or skills center), please mention this information as well. When working with a tutor, ask this person to read your notes, related handouts and pertinent sections of the textbook.