

Course Objectives

This course introduces students to selected topics in Number Theory that will reinforce the proof writing skills learned in MATH 260 (Logic & Sets). There is also a fair amount of computation involved that will reinforce the concepts and provide insight and intuition. Fundamentally, Number Theory is the study of divisibility, factorization and primes in the positive integers. This study will lead us to investigate all the integers (positive, negative & zero) and the rational numbers as well. Learner objectives, outcomes and skills include, but are not limited to:

- using the Euclidean Algorithm to find the gcd of a pair of positive integers and solve linear congruence equations
- understanding and using the Fundamental Theorem of Arithmetic to compute and solve a variety of problems
- applying the Chinese Remainder Theorem
- using Fermat's *Little* Theorem (FLT) and Euler's Generalization of FLT
- computing Pythagorean Triples and solving related problems
- solving linear congruence equations
- knowing some of the history, significance and role Fermat's **Last** Theorem has played in mathematics, especially, number theory.

Comments

1. **Exam.** The exam for this course can be broken up into the following five components:

(i) Definitions & Named Theorems:

Logically equivalent statements for definitions and *any theorem that has a name*.

(ii) Basic proofs:

You should know any proof I give in class that is starred: **proof***.

(iii) True – False

You know what true – false questions are like.

(iv) Computations:

Routine computations similar to HW problems.

(v) Original proofs:

Routine proofs similar to HW problems.

2. **Extra Credit.** Extra Credit in your packet is marked with an asterisk (e.g., 4*). These problems are not restricted to your packet – find an interesting and non-routine problem in Dudley's book, and then ask me if it is appropriate. Even better, if you have found your own pattern and you think you can prove it, submit it.

In general, consult with me on any problem you find interesting.

There is an extra special extra credit worth 50 to 70 HW points. Ask me for details.

Deadline for extra credit is 10 days after that topic has been covered.

N.B., All Extra Credit must be *individual* work – no joint work or other collaborations.

3. **Expository Paper.** An expository paper/project, minimum six pages and three works cited, can be submitted in lieu of the Final Exam. Deadline for topic approval is Friday, May 12. Team projects (two students) are welcome. Students must have a B or better to pursue this option. Details and paper/project suggestions will be given upon request.

4. **Homework Protocol** Ideally, homework should be done individually. However, your MATH 430 professor understands the value of collaborative work or receiving help from someone other than yours truly. All I ask of you is that you document those from whom you received assistance. In these cases please write at the beginning of your homework paper:

(i) "I received help (assistance, hints) on problem(s) _____ from _____."

or

(ii) " 'Ethan' and I worked together on problem(s) _____."